

WORD PROBLEMS: LINEAR EQUATIONS.

1. Kate took 5 hours to travel the 250km from Auckland to Taupo.
Her average speed for the 1st 3 hours is v km/h
Her average speed for the last 2 hours was **10 km/h less** than for the 1st 3 hours.
Find her average speed during the 1st 3 hours of the trip.

2. My son is 31 years younger than me.
In 1 year's time, my son's age will be one quarter of my current age.
How old am I now?

3. A field is length x m and the width is 12m less.
If I add 30m to the length and the width, the perimeter doubles.
Find the original dimensions of the field.

4. A chocolate shake costs \$2 less than a smoothie.
If 5 chocolate shakes and 3 fruit smoothies cost \$30, find the cost of a smoothie.

5. If Jo walks 6km at x km/h and 10 km at $(2x)$ km/hour her journey takes a total of 2 hours.
Form an equation and solve it to find x .

Applications. Linear equations **ANSWERS**

1. Kate took 5 hours to travel the 250km from Auckland to Taupo.

Her average speed for the 1st 3 hours is v km/h

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Find her average speed during the 1st 3 hours of the trip.

Let speed for 1st 3 hours be v km/h so distance = speed \times time = $3v$

Distance for 2nd 2 hours = $2(v - 10)$

Total dist = $2v - 20 + 3v = 250$

$$5v = 270$$

$$v = 54 \text{ km/h}$$

2. My son is 31 years younger than me. In 1 year's time, my son's age will be one quarter of my current age. How old am I now?

Let my age = x so son is $x - 31$

When I am $x + 1$ his age is $x - 30$ and is $\frac{1}{4}$ of my current age = $x/4$

$$\frac{x - 30}{4} = \frac{x}{4}$$

$$x - 30 = x$$

$$x = 4x - 120$$

$$120 = 3x$$

$$x = 40$$

3. A field is length x m and the width is 12m less. If I add 30m to the length and the width, the perimeter doubles. Find the original dimensions of the field.

Length = x width = $x - 12$ so perimeter = $2(2x - 12) = 4x - 24$

If length = $x + 30$ and width = $x + 18$ perimeter = $2(2x + 48) = 4x + 96$

If this is doubled then

$$4x + 96 = 2(4x - 24)$$

$$4x + 96 = 8x - 48$$

$$144 = 4x$$

$$x = 36 \text{ m}$$

length = 36 m, width = 24 m

4. A chocolate shake costs \$2 less than a smoothie. 5 chocolate shakes and 3 fruit smoothies cost \$30. Find the cost of a smoothie.

Let choc shake costs x , smoothie costs $x + 2$

$$5x + 3(x + 2) = 30$$

$$8x + 6 = 30$$

$$8x = 24$$

$$x = 3 \quad \text{choc shake} = \$3 \quad \text{smoothie} = \$5$$

5. If Jo walks 6km at x km/h and 10 km at $(2x)$ km/hour her journey takes a total of 2 hours. Form an equation and use it to solve it to find x .

$$\text{Time} = \frac{6}{x} + \frac{10}{2x} = 2 \quad \text{so} \quad \frac{6}{x} + \frac{5}{x} = 2$$

$$\text{so } \frac{11}{x} = 2 \quad \text{so } x = \frac{11}{2} = 5.5 \text{ km/h}$$